A Framework for Achieving KDM-CCA Secure Public-Key Encryption

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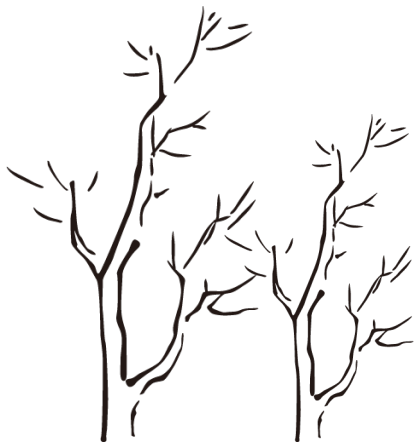

Security notions for PKE

- It has been considered "IND-CCA security = standard"
  - takes active adversaries into consideration
  - implies non-malleability

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e.g.) Anonymous credential, hard-disk encryption, FHE…

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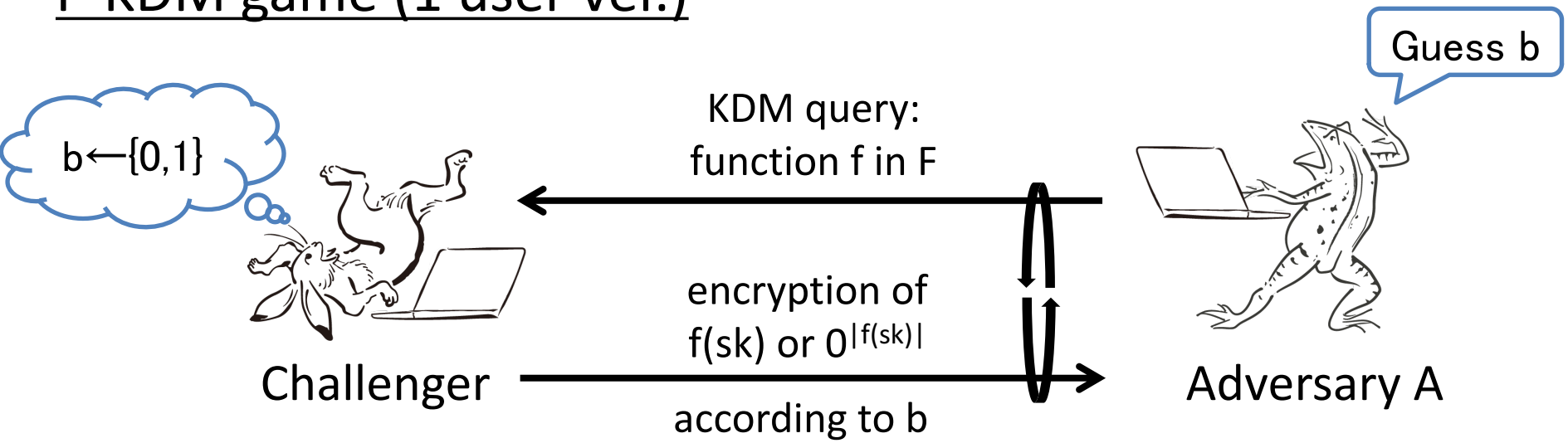
Key dependent message (KDM) security [BRS02]

KDM security

F-KDM game (1 user ver.)



A cannot guess b correctly with prob. greater than 1/2 $\Rightarrow$ F-KDM-CPA secure

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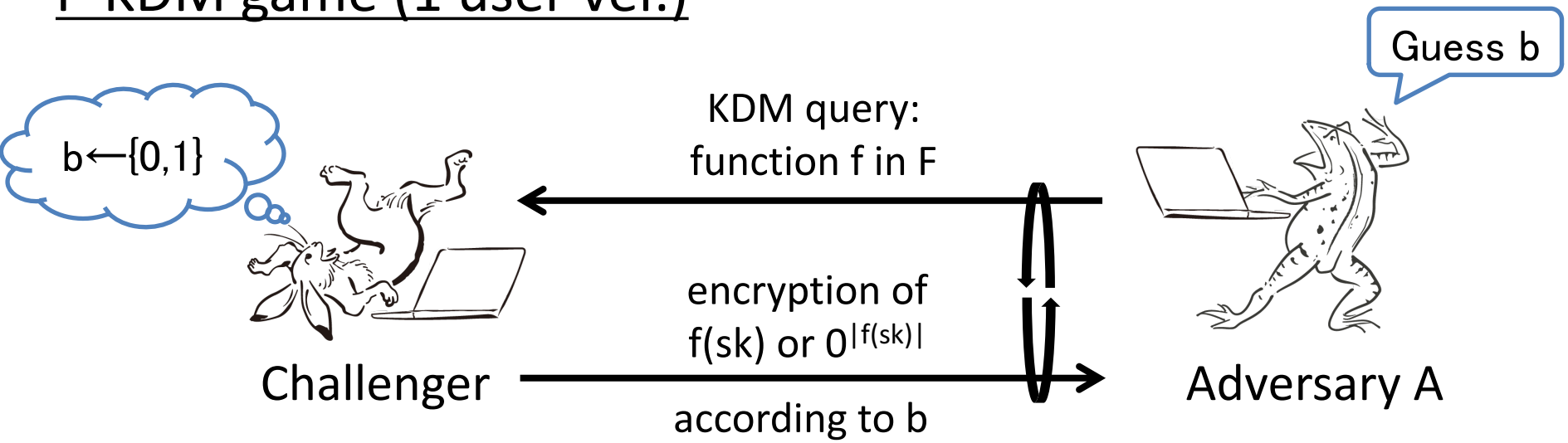


A cannot guess b correctly with prob. greater than 1/2 $\Rightarrow$ F-KDM-CPA secure

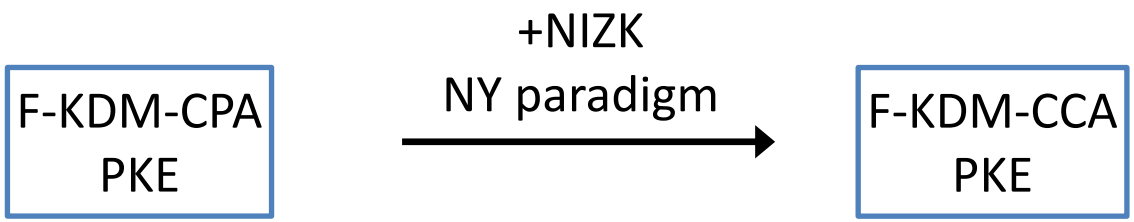
- The adversary can also make a decryption query
  $\Rightarrow$ F-KDM-CCA secure

Our focus

Previous works on KDM-CCA

1. [CCS09]

F: any function class



Concrete instantiation: Aff-KDM-CCA PKE from DDH on pairing

Previous works on KDM-CCA

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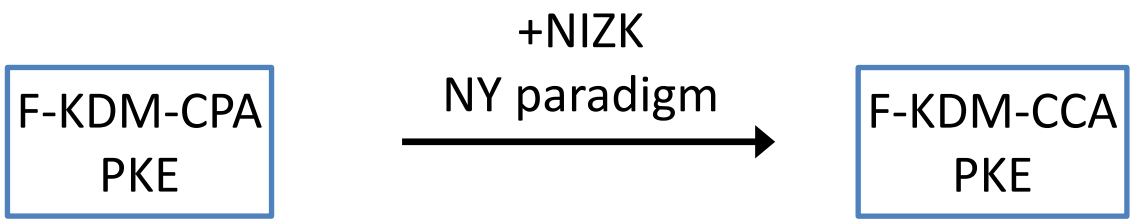

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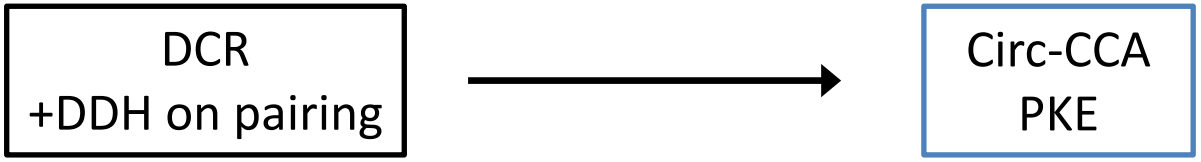
2. [Hof13]



More efficient than [CCS09]

Previous works on KDM-CCA

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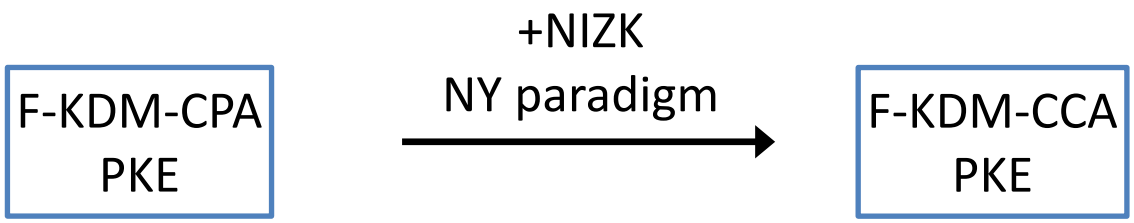

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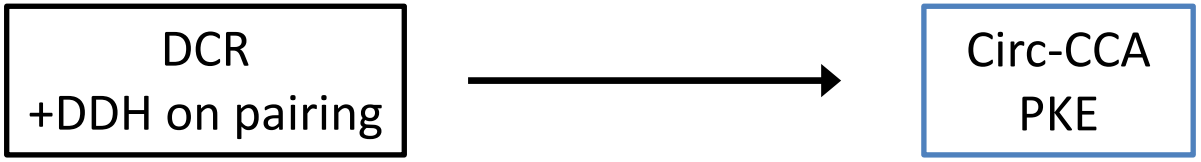
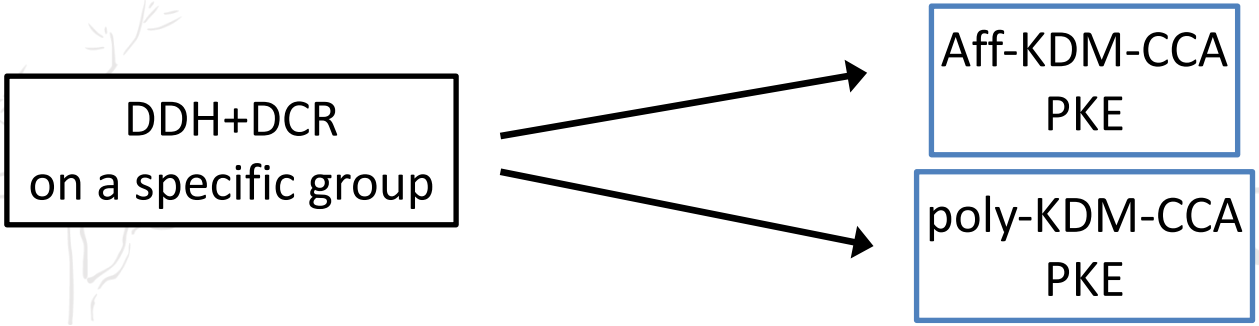


More efficient than [CCS09]

3. [HLL16] (based on [LLJ15])



w/o pairing and efficient

Open problem

ALL existing KDM-CCA secure PKE rely on [NIZK or pairing or multiple assumptions (DDH+DCR)]

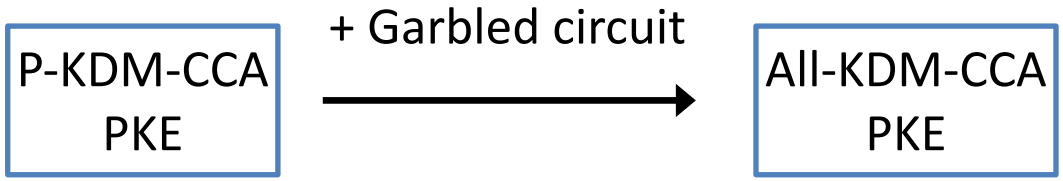
Especially,
all schemes w/o NIZK are proposed under DDH+DCR on a specific group
→ Removing one of them seems to be difficult

Construction based on a single assumption using neither NIZK nor pairing??

KDM-CCA for all functions

[App11] showed

P-KDM: KDM security w.r.t. projection functions

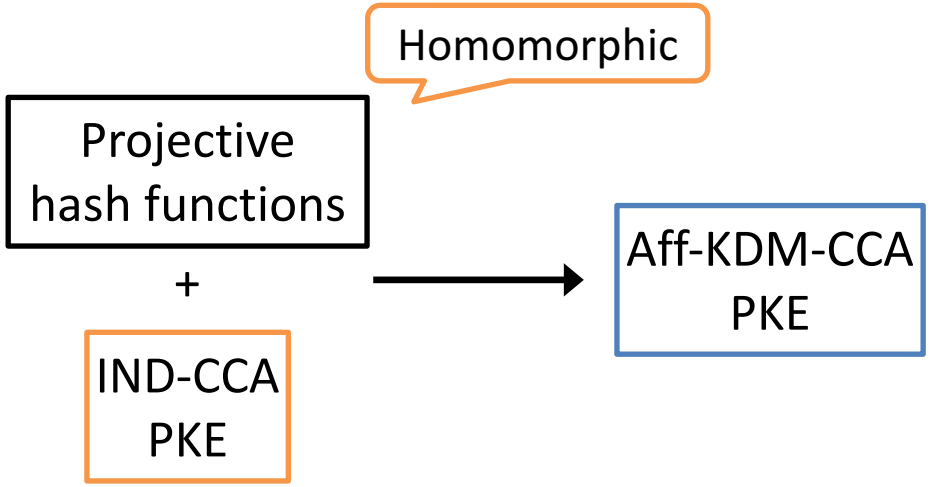


Only [CCS09]'s scheme is compatible with this transformation
→ Need NIZK or pairing

All-KDM-CCA secure PKE
using neither NIZK nor pairing??

This work

1. A framework achieving KDM-CCA security in 1 user setting



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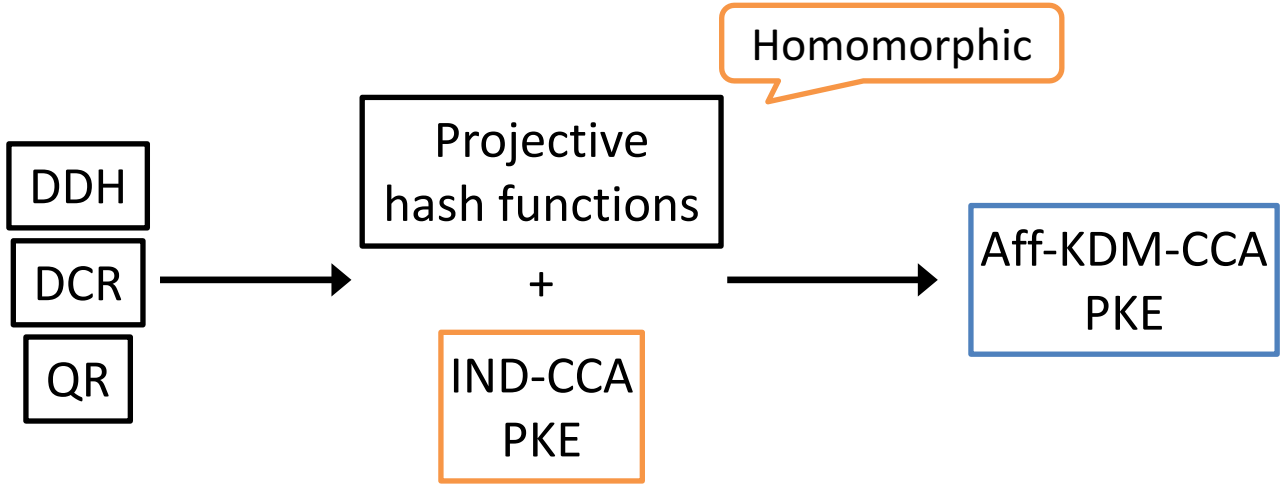

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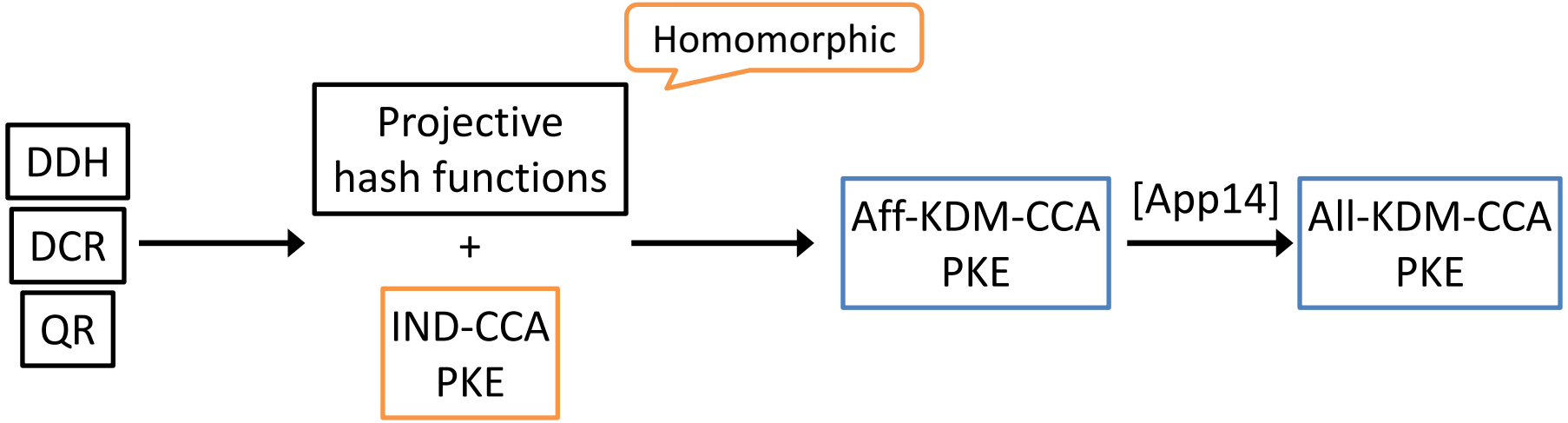

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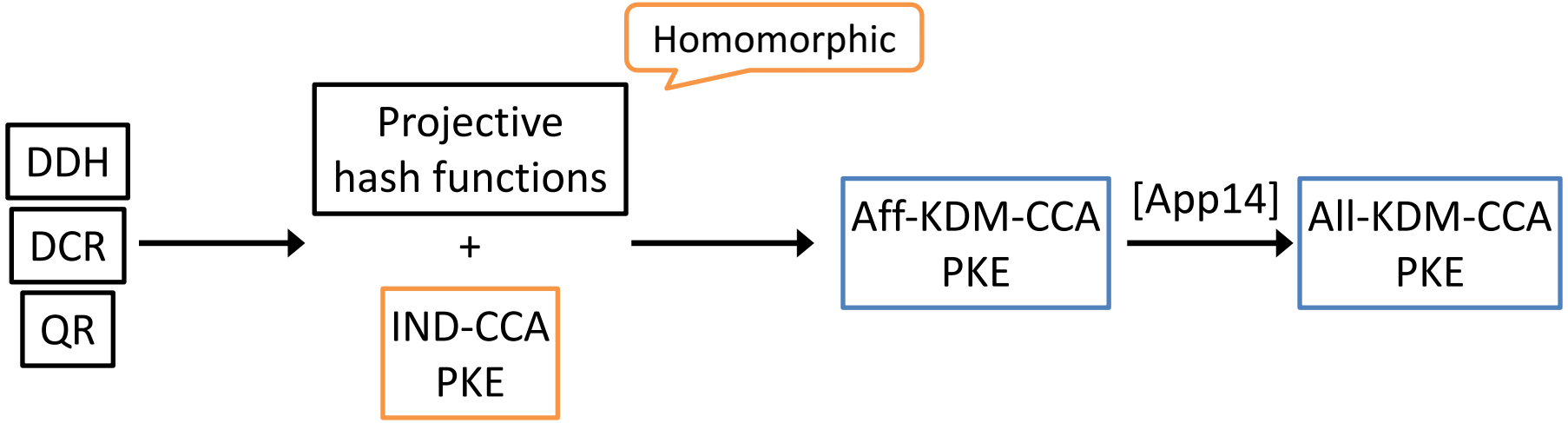
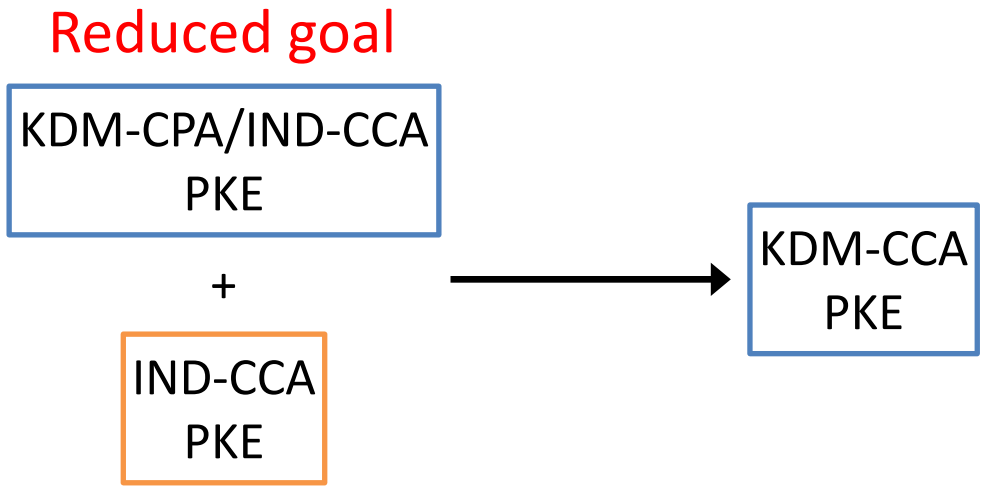


2. KDM-CCA security in multi user setting of concrete instantiations

Reduced goal

We essentially show



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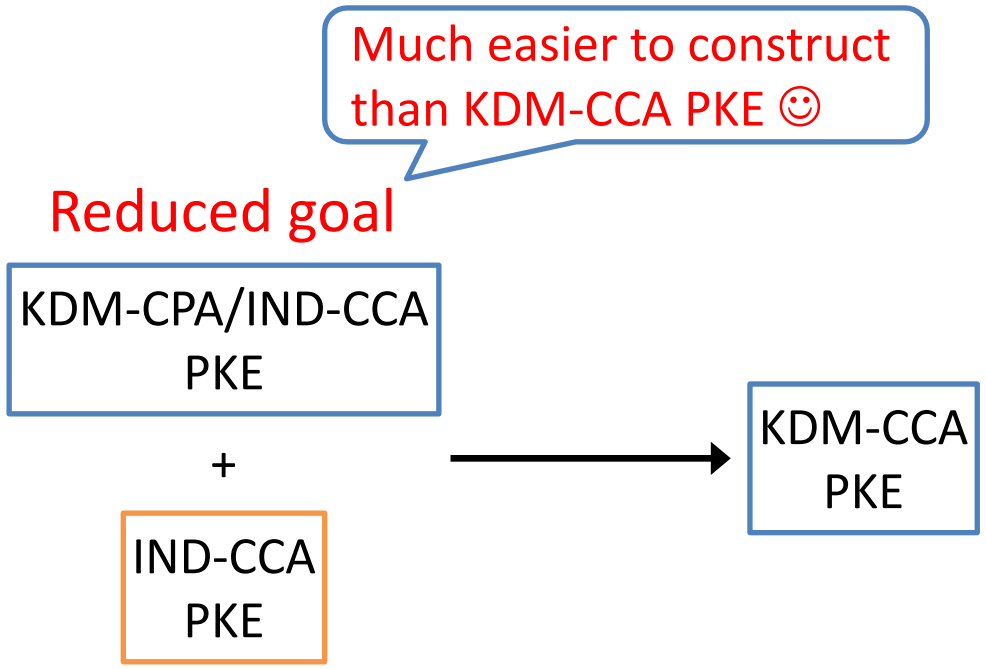

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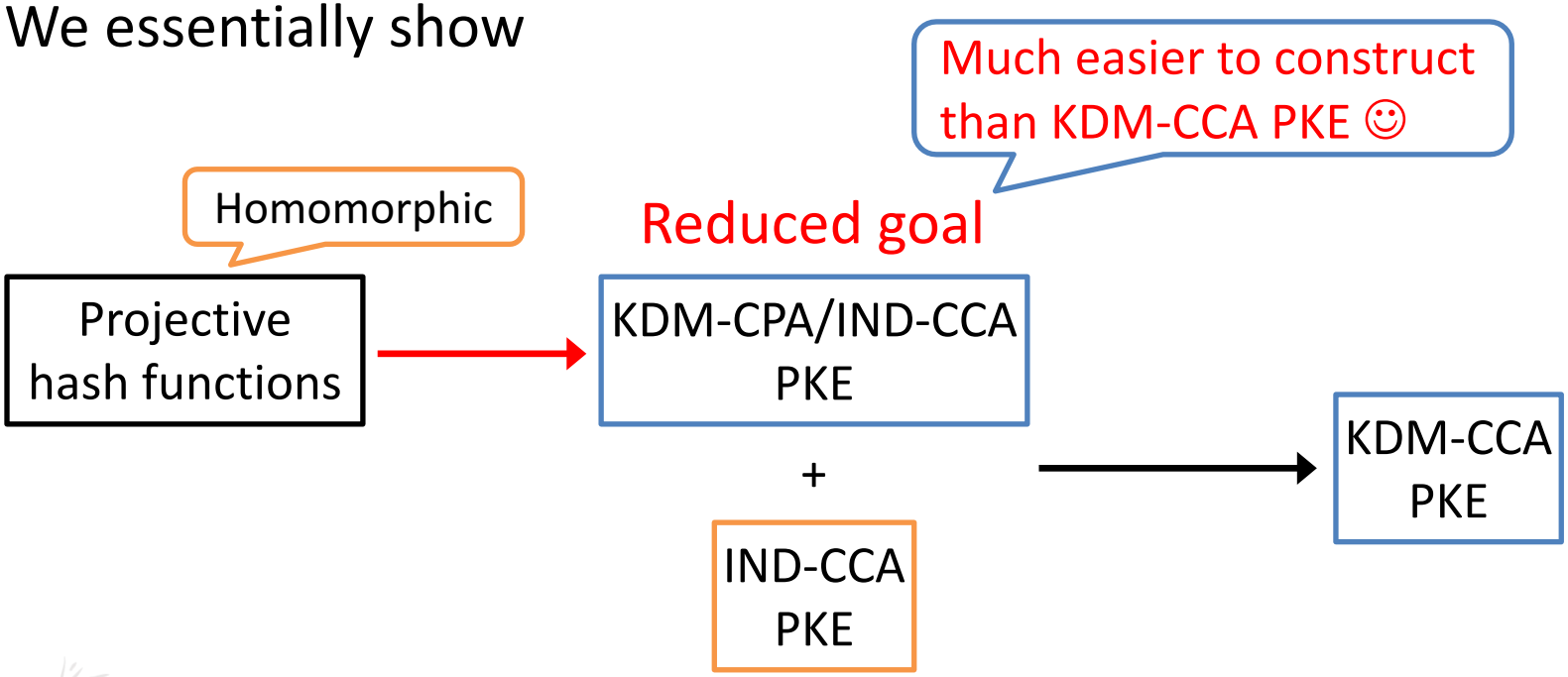

Triple mode proof [MTY11]

- Framework for proving KDM-CPA

Standard mode

$\mathsf{E}(\mathsf{pk}, f(\mathsf{sk}))$

It is difficult to directly prove it based on the secrecy of secret-key… ☹

Hide mode

$\mathsf{E}(\mathsf{pk}, 0)$

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Complete entire proof ☺

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Reduction does not need it ☺

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Extension to CCA setting

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→ Reduction knows secret-key

→ This step goes through when proving KDM-CCA ☺

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We need new technique

First try

$$\mathsf{E}_{\mathsf{cca}}(\mathsf{pk}_{\mathsf{cca}}, \mathsf{E}(\mathsf{pk}, m))$$

Outer scheme: IND-CCA

Inner scheme: KDM-CPA

Shown using triple mode proof

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Using IND-CCA of outer scheme

Reduction can use

- sk of inner scheme
- decryption oracle for outer scheme

→ Simulate decryption oracle ☺

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But, this idea has a problem…

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How to maintain sk_{cca}??

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Fake mode

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If we maintain sk_{cca} as a part of secret-key

$f(sk||sk_{cca})$ is encrypted

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Not KDM secure

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⇨ We can do it if inner scheme is also IND-CCA

Remove circularity

- We maintain $\mathsf{sk}_{\mathsf{cca}}$ as a part of public-key after encrypted by inner scheme

Public-key: $(\mathsf{pk}, \mathsf{pk}_{\mathsf{cca}}, \mathsf{E}(\mathsf{pk}, \mathsf{sk}_{\mathsf{cca}}))$

Secret-key: sk

Encryption: $\mathsf{E}_{\mathsf{cca}}(\mathsf{pk}_{\mathsf{cca}}, \mathsf{E}(\mathsf{pk}, m))$

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Eliminate it before step (2)
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Hide mode

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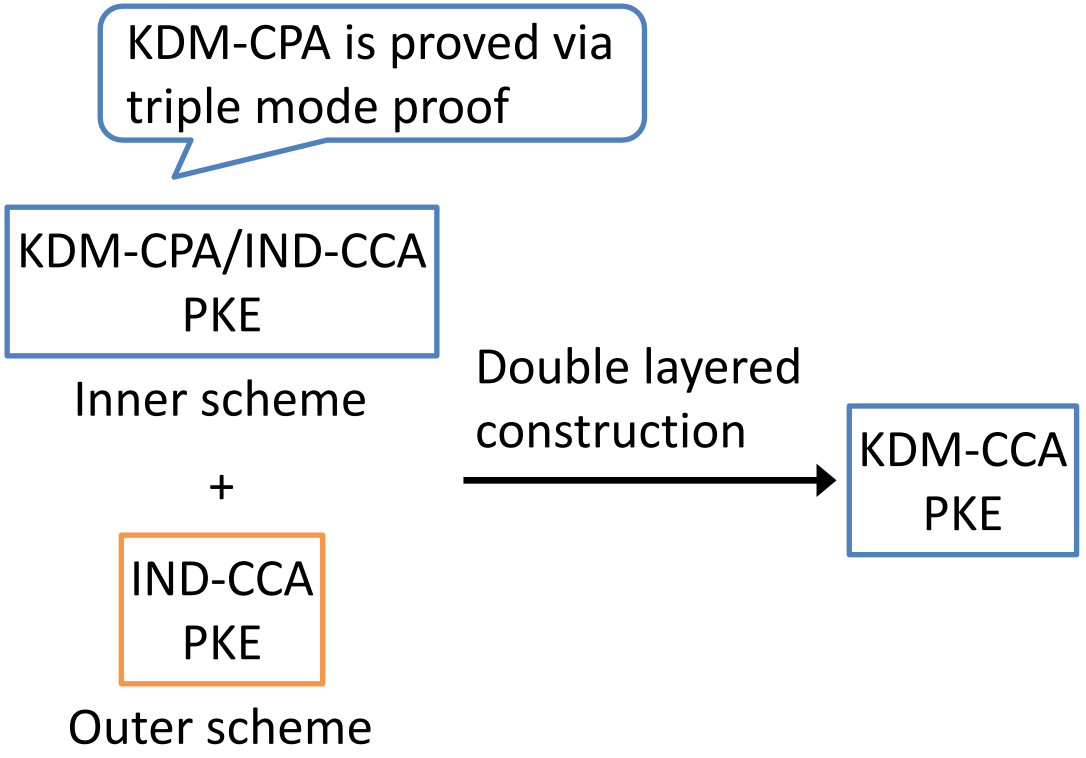
Using IND-CCA of outer scheme

Complete entire proof ☺

Reduced goal



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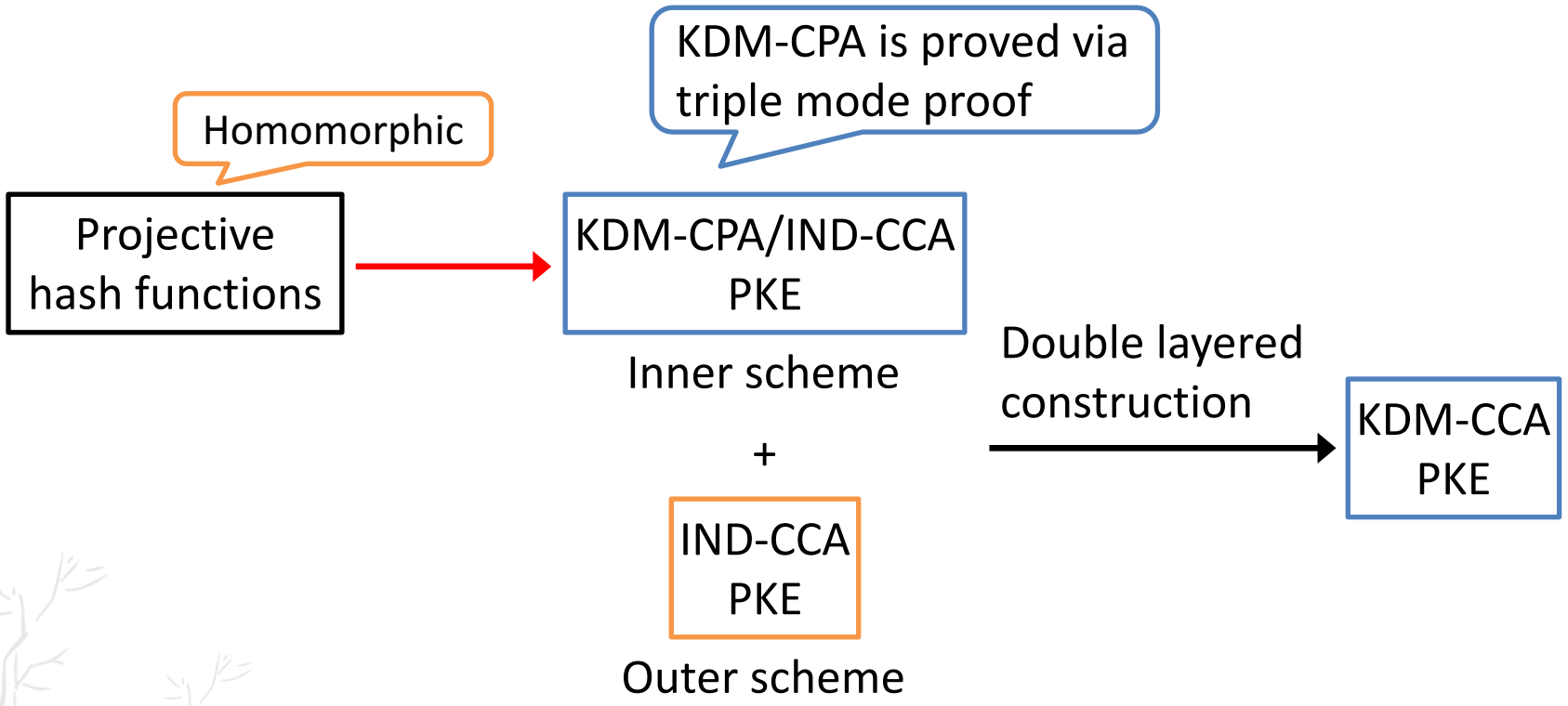

Inner scheme from PHF

- Extend [Wee16] that is a generalization of [BHHO08,BG10]

Homomorphic and Smooth PHF

KDM-CPA PKE

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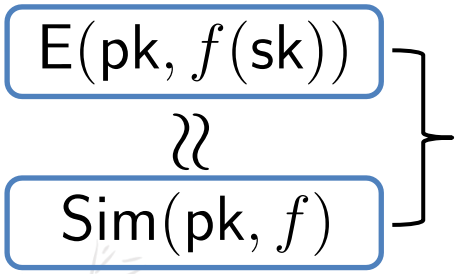
Homomorphic and Smooth PHF ⇨ KDM-CPA PKE

- KDM-CPA of Wee's scheme can be shown using triple mode proof



Homomorphism
projective property
Subset membership problem

Using the secrecy of encryption randomness

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- It is also IND-CPA

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Smoothness
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Homomorphic and Smooth PHF + [CS02] Universal PHF ⇨ KDM-CPA PKE

Also IND-CCA

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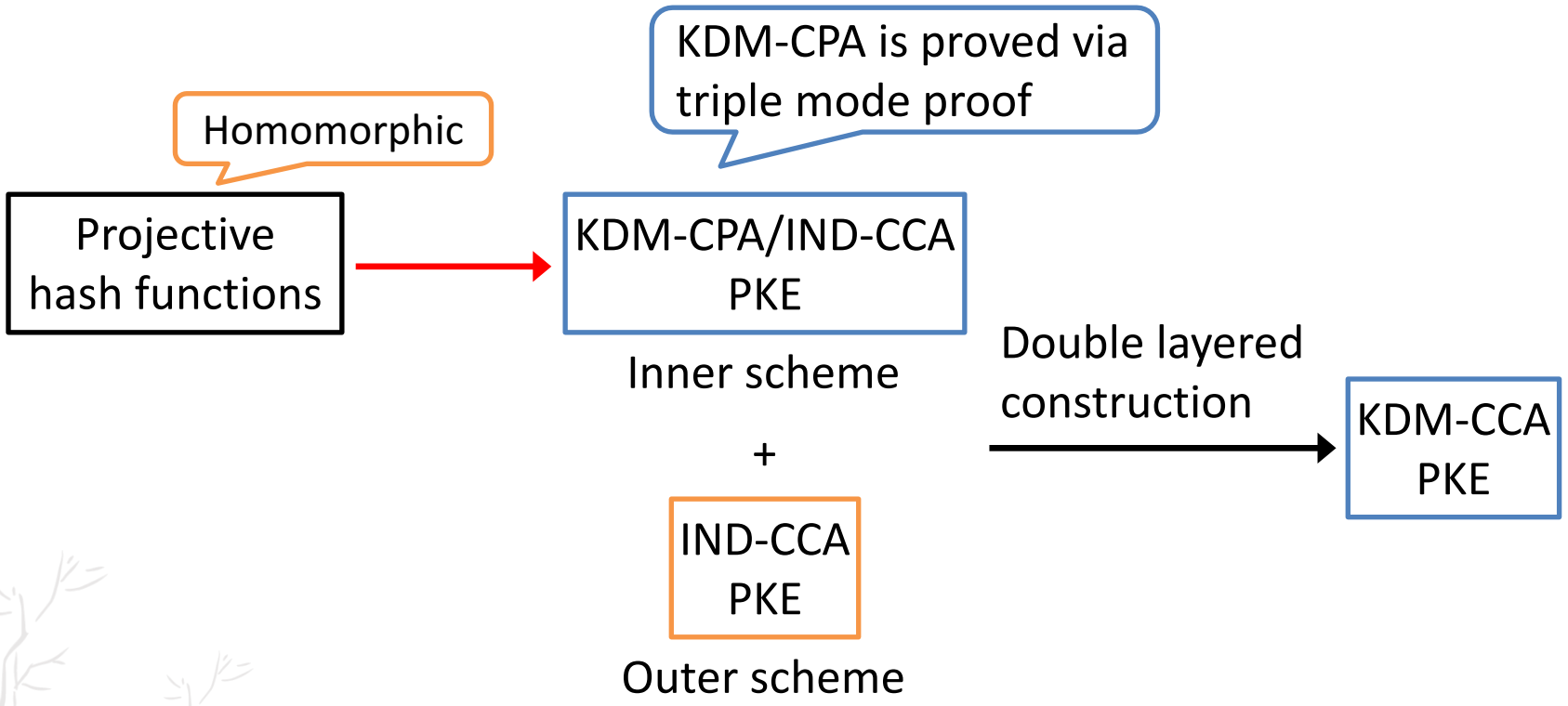
Smoothness
Subset membership problem

By using universal PHF,
we can upgrade it into IND-CCA ☺

Our generic construction



Instantiations and multi-user security

Instantiations

We can instantiate inner scheme based on instantiations of [Wee16]

DDH [BHHO08]

DCR/QR [BG10]

Instantiations and multi-user security

Instantiations

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DDH [BHHO08]
DCR/QR [BG10]

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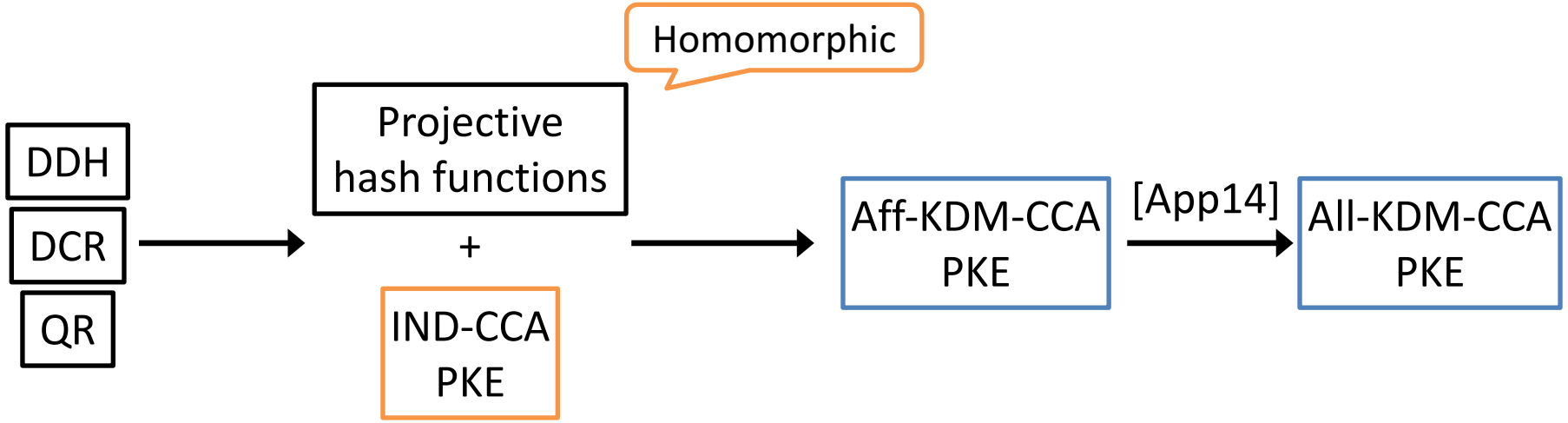
Our instantiations are extensions of [BHHO08, BG10]

Using similar technique as them,
we can prove multi-user security ☺

Summary

1. A framework achieving KDM-CCA security in 1 user setting



2. KDM-CCA security in multi user setting of concrete instantiations